# MULTIPLE ACCESS STEGANOGRAPHIC METHOD BASED ON CODE CONTROL AND FREQUENCY ARRANGEMENTS 

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#### Abstract

The development, as well as the wider practical application of modern steganography, leads to the need to create steganographic methods with multiple access, which would be able to ensure the simultaneous transmission and division of information from several users in a steganographic channel. The currently known multiple-access steganographic methods are based on MC-CDMA technology and do not show how exactly the embedding and extraction of additional information should be performed. The purpose of this paper is to develop a multiple-access steganographic method based on code control and frequency arrangements. This purpose was achieved through the development of a steganographic method with code control and the use of frequency arrangements based on double-cyclic Reed-Solomon codes over Galois fields $\mathrm{GF}(\mathrm{q})$, which provides separate embedding of information by each user at any time which is convenient for him using a personal frequency arrangement. It was proposed to construct the frequency arrangements on the basis of Reed-Solomon codes over the Galois fields $\mathrm{GF}(5)$ and $\mathrm{GF}(13)$. The characteristics of the developed method are researched, within which it is shown that the PSNR of the resulting steganographic message depends on the number of users simultaneously transmitting information through the steganographic channel. With the number of simultaneously operating users $\mathrm{N} \leq 8$, the PSNR values remain at an acceptable level. During the operation of the proposed steganographic method, the occurrence of intra-system interference in the steganographic channel was detected with the number of users simultaneously transmitting information $\mathrm{N}>\mathrm{q}$, however, when using frequency arrangements based on the Reed-Solomon code over the GF(13), their effect is insignificant with a practically justified number of divided channels. The developed steganographic method is a rational solution if it is necessary to organize a steganographic channel with multiple access and can provide flexible resource allocation: the operation of the required number of users with a given bandwidth and the required perception reliability.


Keywords: steganography, code control, multiple access, code division, frequency arrangement.

## Introduction and statement of the problem

Steganography is one of the most important components of modern information security systems [1], which not only makes it impossible to read information without the presence of a secret key, but also allows to hide the very fact of secret information transference. The rapid development of the theory and practice of steganography, which is currently taking place, has led to the emergence of many effective steganographic methods with a high level of performance [2], resistance to common attacks (lossy compression, noise, blurring, scaling, etc.) [3...6], as well as providing a high level of reliability of steganographic message perception [7]. A property of these methods is the ability to transmit additional information in a steganographic message, intended for one specific user.

Nevertheless, in order to solve some practical tasks [8, 9], it becomes necessary to transmit in one steganographic message information intended for more than one user, i.e. organize in the steganographic channel a multiple access. One of the effective methods for solving this problem is the use of MC-CDMA technology using the Walsh-Hadamard transform, which was proposed in [8], and was further developed in [10]. The disadvantages of this technology include the fact that the number of users is strictly regulated and equal to $N=2^{k}=2,4,8,16, \ldots$. MC-CDMA
technology does not show exactly how the embedding and extraction of additional information should be performed, which is another significant disadvantage of the mentioned method of code division of channels.

As it is shown in this paper, the mentioned disadvantages of using MC-CDMA technology in steganographic methods can be eliminated by combining the advantages of the steganographic method with code control, as well as the frequency arrangement technology used to build asynchronous address communication systems based on time-frequency matrices (TFM signals) [11]. Such signals are used in terrestrial, satellite and other communication systems, in command radio control systems as well as in the air traffic control systems.

The purpose of this paper is to develop a multiple-access steganographic method based on code control and frequency arrangements.

## Definitions and constructions

The proposed in this paper method uses the relationship established in [3] between the twodimensional and one-dimensional Walsh-Hadamard transforms: up to a coefficient $1 / N$, the twodimensional Walsh-Hadamard transform $W=H^{\prime} X H^{\prime T}$ can be represented in terms of the onedimensional Walsh-Hadamard transform using the following relation $\tilde{W}=\tilde{X} H_{N_{2}}$, where $H_{N}$ is the Walsh-Hadamard matrix of order $N=2^{k}$, which is constructed according to Sylvester's construction

$$
H_{2^{k}}=\left[\begin{array}{c}
H_{2^{k-1}}  \tag{1}\\
H_{2^{k-1}}-H_{2^{k-1}} \\
H^{k-1}
\end{array}\right], H_{1}=1,
$$

while $H_{N}^{\prime}=\frac{1}{\sqrt{N}} H_{N}$, and operator $\tilde{A}$ denotes writing the matrix $A$ of order $N \times N$ as a row vector of length $N^{2}$ by sequential rows concatenation.

As the basis of the developed steganographic method with multiple access, it is proposed to use the steganographic method with the code control [3], the main idea of which is to use the linearity property of the Walsh-Hadamard transform

$$
\begin{gather*}
\tilde{M}=\tilde{X}+\tilde{D} \\
\tilde{M} H_{N^{2}}=\tilde{X} H_{N^{2}}+\tilde{D} H_{N^{2}}, \tag{2}
\end{gather*}
$$

where $X$ is a block of a matrix-container of size $\mu \times \mu, D$ is a block of additional information of size $\mu \times \mu, M$ is a block of a steganographic message of size $\mu \times \mu$. In this paper we consider the block size $\mu \times \mu=8 \times 8$.

Using additional coding of the matrix $D$ with codes having a given form of WalshHadamard transform coefficients, it is possible to embed the additional information into a given Walsh-Hadamard transform coefficient of the container image $X$. Thus, by modifying the codewords that represent the bits of the steganographic message, it is possible to manipulate the properties of the steganographic method: the embedding of information into medium or low frequencies makes it possible to achieve resistance to attacks by compression, noise, and
blurring, while the embedding of information into higher frequency components allows a higher probability to guarantee the reliability of the steganographic message perception.

In [3], an explicit correspondence was established between the transformants of the WalshHadamard transform, as well as transformants of the discrete cosine transform (DCT), which has the following form for the case of the size of transformations $\frac{\mu}{2} \times \frac{\mu}{2}=4 \times 4$

| DCT | Walsh-Hadamard |  | DCT | Walsh-Hadamard |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Transform |  |  | Transform |
| $(1,1)$ | $\leftrightarrow$ | $(1,1)$ | $(3,1)$ | $\leftrightarrow$ | $(4,1)$ |
| $(1,2)$ | $\leftrightarrow$ | $(1,3)$ | $(3,2)$ | $\leftrightarrow$ | $(4,2)$ |
| $(1,3)$ | $\leftrightarrow$ | $(1,4)$ | $(3,3)$ | $\leftrightarrow$ | $(4,4)$ |
| $(1,4)$ | $\leftrightarrow$ | $(1,2)$ | $(3,4)$ | $\leftrightarrow$ | $(4,2)$ |
| $(2,1)$ | $\leftrightarrow$ | $(3,1)$ | (4,1) | $\leftrightarrow$ | $(2,1)$ |
| $(2,2)$ | $\leftrightarrow$ | $(3,3)$ | $(4,2)$ | $\leftrightarrow$ | $(2,3)$ |
| $(2,3)$ | $\leftrightarrow$ | $(3,4)$ | $(4,3)$ | $\leftrightarrow$ | $(2,4)$ |
| $(2,4)$ | $\leftrightarrow$ | $(3,2)$ | $(4,4)$ | $\leftrightarrow$ | $(2,2)$ |

For example, to ensure the reliability of perception, the embedding of information must be done so that just the most high-frequency Walsh-Hadamard transformants undergo modifications.

In Table 1, we present the codewords used in the steganographic method developed in this paper, which affect the transformants $(1,2) ;(1,4) ;(2,1) ;(2,2) ;(2,3) ;(2,4) ;(3,2) ;(3,3) ;(3,4)$; $(4,1) ;(4,2) ;(4,3) ;(4,4)$ (excluding the lowest-frequency transformants $(1,1) ;(1,3) ;(3,1))$.

Table 1
Codewords aimed at modifying the given Walsh-Hadamard transformant

| $T_{4,(1,2)}^{+}$ | $T_{4,(1,4)}^{+}$ | $T_{4,(2,1)}^{+}$ | $T_{4,(2,2)}^{+}$ |
| :---: | :---: | :---: | :---: |
| $\left[\begin{array}{llll}1 & -1 & 1 & -1 \\ 1 & -1 & 1 & -1 \\ 1 & -1 & 1 & -1 \\ 1 & -1 & 1 & -1\end{array}\right]$ | $\left[\begin{array}{llll}1 & -1 & -1 & 1 \\ 1 & -1 & -1 & 1 \\ 1 & -1 & -1 & 1 \\ 1 & -1 & -1 & 1\end{array}\right]$ | $\left[\begin{array}{rrrr}1 & 1 & 1 & 1 \\ -1 & -1 & -1 & -1 \\ 1 & 1 & 1 & 1 \\ -1 & -1 & -1 & -1\end{array}\right]$ | $\left[\begin{array}{rrrr}1 & -1 & 1 & -1 \\ -1 & 1 & -1 & 1 \\ 1 & -1 & 1 & -1 \\ -1 & 1 & -1 & 1\end{array}\right]$ |
| $T_{4,(2,3)}^{+}$ | $T_{4,(2,4)}^{+}$ | $T_{4,(3,2)}^{+}$ | $T_{4,(3,3)}^{+}$ |
| $\left[\begin{array}{rrrr}1 & 1 & -1 & -1 \\ -1 & -1 & 1 & 1 \\ 1 & 1 & -1 & -1 \\ -1 & -1 & 1 & 1\end{array}\right]$ | $\left[\begin{array}{rrrr}1 & -1 & -1 & 1 \\ -1 & 1 & 1 & -1 \\ 1 & -1 & -1 & 1 \\ -1 & 1 & 1 & -1\end{array}\right]$ | $\left[\begin{array}{rrrr}1 & -1 & 1 & -1 \\ 1 & -1 & 1 & -1 \\ -1 & 1 & -1 & 1 \\ -1 & 1 & -1 & 1\end{array}\right]$ | $\left[\begin{array}{rrrr}1 & 1 & -1 & -1 \\ 1 & 1 & -1 & -1 \\ -1 & -1 & 1 & 1 \\ -1 & -1 & 1 & 1\end{array}\right]$ |
| $T_{4,(3,4)}^{+}$ | $T_{4,(4,1)}^{+}$ | $T_{4,(4,2)}^{+}$ | $T_{4,(4,3)}^{+}$ |
| $\left[\begin{array}{cccc}1 & -1 & -1 & 1 \\ 1 & -1 & -1 & 1 \\ -1 & 1 & 1 & -1 \\ -1 & 1 & 1 & -1\end{array}\right]$ | $\left[\begin{array}{rrrr}1 & 1 & 1 & 1 \\ -1 & -1 & -1 & -1 \\ -1 & -1 & -1 & -1 \\ 1 & 1 & 1 & 1\end{array}\right]$ | $\left[\begin{array}{rrrr}1 & -1 & 1 & -1 \\ -1 & 1 & -1 & 1 \\ -1 & 1 & -1 & 1 \\ 1 & -1 & 1 & -1\end{array}\right]$ | $\left[\begin{array}{rrrr}1 & 1 & -1 & -1 \\ -1 & -1 & 1 & 1 \\ -1 & -1 & 1 & 1 \\ 1 & 1 & -1 & -1\end{array}\right]$ |
| $T_{4,(4,4)}^{+}$ | - | - | - |
| $\left[\begin{array}{rrrr}1 & -1 & -1 & 1 \\ -1 & 1 & 1 & -1 \\ -1 & 1 & 1 & -1 \\ 1 & -1 & -1 & 1\end{array}\right]$ | - | - | - |

Such a number of selected frequency components is chosen because of the fact that in this paper we consider the use of two frequency arrangement codes: the first code assumes the largest number of users operating in the system, using 13 frequency components, while the second code uses five frequency components and provides the best reliability of perception.

Note that the application of the codewords presented in Table 1 in accordance with (2) causes a targeted effect on the corresponding Walsh-Hadamard transformant, while the remaining transformants of the steganographic message remain unchanged.

Each codeword shown in Table 1 is the frequency component for the first frequency arrangement code ${ }_{1 i}$ and the second ${ }_{2 i}$, respectively

$$
\begin{array}{llllll}
T_{4,(1,2)}^{+} & \leftrightarrow & f_{10} \\
T_{4,(1,4)}^{+} & \leftrightarrow & & & \\
f_{11} & & & \\
T_{4,(2,1)}^{+} & \leftrightarrow & f_{12} & & & \\
T_{4,(2,2)}^{+} & \leftrightarrow & f_{13} \\
T_{4,(2,3)}^{+} & \leftrightarrow & f_{14} & T_{4,(2,2)} & \leftrightarrow & f_{20} \\
T_{4,(2,4)}^{+} & \leftrightarrow & f_{15} & T_{4,(2,3)} & \leftrightarrow & f_{21}  \tag{4}\\
T_{4,(3,2)}^{+} & \leftrightarrow & f_{16} & T_{4,(2,4)} & \leftrightarrow & f_{22} \\
T_{4,(3,3)}^{+} & \leftrightarrow & f_{17} & T_{4,(3,2)} & \leftrightarrow & f_{23} \\
T_{4,(3,4)}^{+} & \leftrightarrow & f_{18} & T_{4,(4,2)} & \leftrightarrow & f_{24} \\
T_{4,(4,1)}^{+} & \leftrightarrow & f_{19} & & & \\
T_{4,(4,2)}^{+} & \leftrightarrow & f_{110} & & & \\
T_{4,(4,3)}^{+} & \leftrightarrow & f_{111} & & & \\
T_{4,(4,4)}^{+} & \leftrightarrow & f_{112} & & &
\end{array}
$$

These frequency components $f_{i}$ of the size $\frac{\mu}{2} \times \frac{\mu}{2}=4 \times 4$ are used in the developed method as elements to form codewords of size $\mu \times \mu$, which is unique for each user in accordance with the frequency arrangement rule

$$
\begin{array}{|l|l|}
\hline f_{i_{1}} & f_{i_{2}}  \tag{5}\\
\hline f_{i_{3}} & f_{i_{4}} \\
\hline
\end{array}
$$

where the vector of indices $\left[i_{1}, i_{2}, i_{3}, i_{4}\right]$ is unique for each user and is determined by the corresponding frequency arrangement.

In modern asynchronous address communication systems for constructing frequency arrangement codes with good correlation properties, non-binary cyclic Bose-ChaudhuriHocquenghem codes also known as Reed-Solomon codes (RS-codes) [11] have become widespread.

In this paper, considering an example of the block length $\mu \times \mu=8 \times 8$, we present two options for generating the frequency arrangement code: the first one is constructed over the Galois field $G F(13)$, which allows you to ensure the maximum number of users operating in the system while maintaining acceptable perception reliability, and the second one is constructed
over the Galois field $G F(5)$, which allows you to provide the best reliability of perception with a smaller number of users operating in the system.

Let's form the first frequency arrangement code based on the RS-code over the Galois field $G F(13)$ with the following parameters: codeword length $N=12$, number of information digits $K=2$, primitive element $\theta=2$, code distance $d=12-2+1=11$. The generating polynomial of a given code is determined by the following relationship

$$
\begin{gather*}
g(z)=\prod_{i=1}^{d-1}\left(z-\theta^{i}\right)=\prod_{i=1}^{10}\left(z-2^{i}\right)= \\
(z-2)(z-4)(z-8)(z-3)(z-6)(z-12)(z-11)(z-9)(z-5)(z-10)=  \tag{6}\\
11+7 z+12 z^{2}+9 z^{3}+3 z^{4}+4 z^{5}+6 z^{6}+10 z^{7}+5 z^{8}+8 z^{9}+z^{10} .
\end{gather*}
$$

On the basis of the generating polynomial (6), we construct a generating matrix, the first row of which consists of the coefficients of the generating polynomial, the remaining $K-1$ rows are defined as a non-cyclic shift to the right by 1 of the previous row, while all unfilled elements of the generating matrix are considered as equal to 0

$$
G=\left[\begin{array}{rrrrrrrrrrrr}
11 & 7 & 12 & 9 & 3 & 4 & 6 & 10 & 5 & 8 & 1 & 0  \tag{7}\\
0 & 11 & 7 & 12 & 9 & 3 & 4 & 6 & 10 & 5 & 8 & 1
\end{array}\right] .
$$

The first row in the generating matrix $G$ will be called as the basic codeword and will be denoted as ${ }^{C_{1}}$. Based on the property of double cyclicity of RS-codes, we can construct all other codewords by cyclic shifts of the basic codeword in time and frequency. Further, each of the codewords of the RS-code is truncated, as a result of which we obtain its first four symbols that we will use as the frequency arrangement.

In this case, the total number of available frequency arrangements generated using the RScode over the Galois field $G F(q)$ is

$$
\begin{equation*}
J=q(q-1)=13 \cdot 12=156 . \tag{8}
\end{equation*}
$$

For brevity in Table 2 these frequency arrangements are presented with the radix equal to $13(10 \rightarrow A, 11 \rightarrow B, 12 \rightarrow C)$.
Thus, using the method of additional coding of information with codewords (5) using frequency arrangements based on the RS-code, presented in Table 2 it is theoretically possible to provide the operation of 156 users in the steganographic channel.
For example, in this case, the first user in the system will transmit information using a frequency arrangement $[\mathrm{B} 7 \mathrm{C} 9] \rightarrow\left[\begin{array}{cccc}11 & 7 & 12 & 9\end{array}\right]$, on the basis of which, in accordance with (4), we form codewords of the form (5) $\left[\begin{array}{llll}f_{111} & f_{17} & f_{112} & f_{19}\end{array}\right]=\left[\begin{array}{llll}T_{4,(4,3)}^{+}, & T_{4,(3,3)}^{+} ; & T_{4,(4,4)}^{+}, & T_{4,(4,1)}^{+}\end{array}\right]$, where the symbol "," means horizontal concatenation, and the symbol ";" means vertical concatenation.

Thus, the first user in the system encodes information using the following codewords ( $T_{1}^{+}$for transmitting bit " 0 " and $T_{1}^{-}$for transmitting bit " 1 ")

Table 2
Representation of the frequency arrangement code based on the RS-code over the Galois field
$G F(13)$ in the form of cyclic shifts in time and frequency of the basic codeword $C_{1}$

| B7C9 | 7C93 | C934 | 9346 | 346A | 46A5 | 6A58 | A581 | 5810 | 810B | 10B7 | 0B7C |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| C80A | 80A4 | 0A45 | A457 | 457B | 57B6 | 7B69 | B692 | 6921 | 921C | 21C8 | 1C80 |
| 091B | 91B5 | 1 B 56 | B568 | 568C | 68C7 | 8C7A | C7A3 | 7A32 | A320 | 3209 | 2091 |
| 1A2C | A2C6 | 2C67 | C679 | 6790 | 7908 | 908B | 08B4 | 8B43 | B431 | 431A | 31A2 |
| 2B30 | B307 | 3078 | 078A | 78A1 | 8A19 | A19C | 19C5 | 9C54 | C542 | 542B | 42B3 |
| 3C41 | C418 | 4189 | 189B | 89B2 | 9B2A | B2A0 | 2A06 | A065 | 0653 | 653C | 53C4 |
| 4052 | 0529 | 529A | 29AC | 9AC3 | AC3B | C3B1 | 3B17 | B176 | 1764 | 7640 | 6405 |
| 5163 | 163A | 63 AB | 3AB0 | AB04 | B04C | 04C2 | 4C28 | C287 | 2875 | 8751 | 7516 |
| 6274 | 274B | 74BC | 4BC1 | BC15 | C150 | 1503 | 5039 | 0398 | 3986 | 9862 | 8627 |
| 7385 | 385C | 85C0 | 5C02 | C026 | 0261 | 2614 | 614A | 14A9 | 4A97 | A973 | 9738 |
| 8496 | 4960 | 9601 | 6013 | 0137 | 1372 | 3725 | 725B | 25BA | 5BA8 | BA84 | A849 |
| 95A7 | 5A71 | A712 | 7124 | 1248 | 2483 | 4836 | 836C | 36CB | 6CB9 | CB95 | B95A |
| A6B8 | 6B82 | B823 | 8235 | 2359 | 3594 | 5947 | 9470 | 470C | 70CA | 0CA6 | CA6B |

$$
T_{1}^{+}=\left[\begin{array}{rrrr|rrrr}
1 & 1 & -1 & -1 & 1 & 1 & -1 & -1  \tag{9}\\
-1 & -1 & 1 & 1 & 1 & 1 & -1 & -1 \\
-1 & -1 & 1 & 1 & -1 & -1 & 1 & 1 \\
1 & 1 & -1 & -1 & -1 & -1 & 1 & 1 \\
\hline 1 & -1 & -1 & 1 & 1 & 1 & 1 & 1 \\
-1 & 1 & 1 & -1 & -1 & -1 & -1 & -1 \\
-1 & 1 & 1 & -1 & -1 & -1 & -1 & -1 \\
1 & -1 & -1 & 1 & 1 & 1 & 1 & 1
\end{array}\right], \quad T_{1}^{-}=\left[\begin{array}{cccc|cccc}
-1 & -1 & 1 & 1 & -1 & -1 & 1 & 1 \\
1 & 1 & -1 & -1 & -1 & -1 & 1 & 1 \\
1 & 1 & -1 & -1 & 1 & 1 & -1 & -1 \\
-1 & -1 & 1 & 1 & 1 & 1 & -1 & -1 \\
\hline-1 & 1 & 1 & -1 & -1 & -1 & -1 & -1 \\
1 & -1 & -1 & 1 & 1 & 1 & 1 & 1 \\
1 & -1 & -1 & 1 & 1 & 1 & 1 & 1 \\
-1 & 1 & 1 & -1 & -1 & -1 & -1 & -1
\end{array}\right] .
$$

Let us now proceed to the construction of the second frequency arrangement code, for which we construct a RS-code over the Galois field $G F(5)$ with the following parameters: codeword length $N=4$, number of information digits $K=2$, primitive element $\theta=3$, code distance $d=N-K+1=3$. We define the generating polynomial of the given code

$$
\begin{align*}
& g(z)=\prod_{i=1}^{d-1}\left(z-\theta^{i}\right)=\prod_{i=1}^{2}\left(z-3^{i}\right)=  \tag{10}\\
& =(z-3)(z-4)=2+3 z+z^{2} .
\end{align*}
$$

Similarly, to the case of the first frequency arrangement code, based on the generating polynomial (10), we construct the generating matrix

$$
G=\left[\begin{array}{llll}
2 & 3 & 1 & 0  \tag{11}\\
0 & 2 & 3 & 1
\end{array}\right],
$$

on the basis of which we construct all the $J=20$ codewords of the Reed-Solomon code (Table 3). Since each of these codewords has a length $N=4$ that corresponds to construction (5), for this code the codewords do not need to be truncated and can be used unchanged.

Table 3
Representation of the RS-code over the Galois field $G F(5)$

| $C_{1}=\left[\begin{array}{llll}2 & 3 & 1 & 0\end{array}\right]$ | $C_{6}=\left[\begin{array}{llll}3 & 1 & 0 & 2\end{array}\right]$ | $C_{11}=\left[\begin{array}{llll}1 & 0 & 2 & 3\end{array}\right]$ | $C_{16}=\left[\begin{array}{llll}0 & 2 & 3 & 1\end{array}\right]$ |
| :---: | :---: | :---: | :---: |
| $C_{2}=\left[\begin{array}{llll}3 & 4 & 2 & 1\end{array}\right]$ | $C_{7}=\left[\begin{array}{llll}4 & 2 & 1 & 3\end{array}\right]$ | $C_{12}=\left[\begin{array}{llll}2 & 1 & 3 & 4\end{array}\right]$ | $C_{17}=\left[\begin{array}{llll}1 & 3 & 4 & 2\end{array}\right]$ |
| $C_{3}=\left[\begin{array}{llll}4 & 0 & 3 & 2\end{array}\right]$ | $C_{8}=\left[\begin{array}{llll}0 & 3 & 2 & 4\end{array}\right]$ | $C_{13}=\left[\begin{array}{llll}3 & 2 & 4 & 0\end{array}\right]$ | $C_{18}=\left[\begin{array}{llll}2 & 4 & 0 & 3\end{array}\right]$ |
| $C_{4}=\left[\begin{array}{llll}0 & 1 & 4 & 3\end{array}\right]$ | $C_{9}=\left[\begin{array}{llll}1 & 4 & 3 & 0\end{array}\right]$ | $C_{14}=\left[\begin{array}{llll}4 & 3 & 0 & 1\end{array}\right]$ | $C_{19}=\left[\begin{array}{llll}3 & 0 & 1 & 4\end{array}\right]$ |
| $C_{5}=\left[\begin{array}{llll}1 & 2 & 0 & 4\end{array}\right]$ | $C_{10}=\left[\begin{array}{llll}2 & 0 & 4 & 1\end{array}\right]$ | $C_{15}=\left[\begin{array}{llll}0 & 4 & 1 & 2\end{array}\right]$ | $C_{20}=\left[\begin{array}{llll}4 & 1 & 2 & 0\end{array}\right]$ |

A steganographic system with multiple access based on the presented Reed-Solomon code (Table 3) can theoretically ensure the operation of $J=20$ users with help of five frequency components.

## Algorithms for embedding and extraction of information

Based on the theoretical material presented, we will describe algorithms for embedding and extraction of information for the developed steganographic method with multiple access.

Information embedding algorithm
Step 1. An ensemble of codewords of size $\frac{\mu}{2} \times \frac{\mu}{2}$ is formed (Table 1), which are acting purposefully on the given transformants of the Walsh-Hadamard transform, as well as an ensemble of frequency arrangements based on the RS-code over the Galois field $G F(q)$ (Table 2 or Table 3). The choice of the base $q$ depends on the number of users operating in the system, as well as on the number of modified Walsh-Hadamard transformants participating in the transmission of information.

Step 2. To each user $A_{z}, z=1,2, \ldots, J$ registered in the steganographic system, a frequency arrangement is allocated for transmitting information over the steganographic channel. On the basis of given frequency arrangement, in accordance with construction (5) and Table 1, the user generates codewords $T_{z}^{+}$and $T_{z}^{-}$of size $\mu \times \mu$.

Step 3. Each of the users $A_{z}$ splits the container image into blocks of size $\mu \times \mu$ and embeds one bit $d_{z, k}$ of the additional information into each of the container blocks $X_{k}$ by applying the summation operation, i.e. each block of a steganographic message is calculated as

$$
\begin{equation*}
M_{k}=X_{k}+D_{k} . \tag{12}
\end{equation*}
$$

The undoubted advantage of the developed steganographic method is the fact that different users, using their frequency arrangements, can embed information independently of each other at any time convenient for them. The number of subscribers simultaneously operating in the system can also be easily scaled.

Let's consider a specific example of information embedding using the developed steganographic method.

Let an ensemble of codewords of size $4 \times 4$ to be formed, which consists of codewords $T_{4,(2,2)}, T_{4,(2,3)}, T_{4,(2,4)}, T_{4,(3,2)}, T_{4,(4,2)}$, as well as an ensemble of frequency arrangements (Table 2). Consider the operation of two users $A_{1}$ and $A_{2}$ with the following frequency arrangements: $C_{1}=\left[\begin{array}{llll}2 & 3 & 1 & 0\end{array}\right]$ and $C_{2}=\left[\begin{array}{llll}3 & 4 & 2 & 1\end{array}\right]$. Let these users perform embedding of information bits $d_{1, k}=1, d_{2, k}=-1$ into the block of the container image

$$
X_{k}=\left[\begin{array}{llllllll}
213 & 214 & 215 & 216 & 215 & 214 & 214 & 214  \tag{13}\\
214 & 215 & 215 & 216 & 215 & 214 & 216 & 214 \\
214 & 214 & 215 & 215 & 214 & 213 & 214 & 214 \\
215 & 215 & 216 & 217 & 214 & 214 & 214 & 214 \\
214 & 214 & 215 & 215 & 214 & 217 & 216 & 216 \\
214 & 214 & 215 & 215 & 216 & 216 & 214 & 216 \\
215 & 216 & 215 & 216 & 215 & 215 & 214 & 216 \\
214 & 216 & 215 & 214 & 215 & 215 & 216 & 215
\end{array}\right] .
$$

On the basis of a given frequency arrangement $C_{1}$, as well as an ensemble of codewords of size $4 \times 4$, the first user generates codewords of size $8 \times 8$ intended for transmitting an additional information bit ${ }_{1, k}$

$$
T_{1}^{+}=\left[\begin{array}{rrrr|rrrr}
1 & -1 & -1 & 1 & 1 & -1 & 1 & -1  \tag{14}\\
-1 & 1 & 1 & -1 & 1 & -1 & 1 & -1 \\
1 & -1 & -1 & 1 & -1 & 1 & -1 & 1 \\
-1 & 1 & 1 & -1 & -1 & 1 & -1 & 1 \\
\hline 1 & 1 & -1 & -1 & 1 & -1 & 1 & -1 \\
-1 & -1 & 1 & 1 & -1 & 1 & -1 & 1 \\
1 & 1 & -1 & -1 & 1 & -1 & 1 & -1 \\
-1 & -1 & 1 & 1 & -1 & 1 & -1 & 1
\end{array}\right], \quad T_{1}^{-}=\left[\begin{array}{rrrr|rrrr}
-1 & 1 & 1 & -1 & -1 & 1 & -1 & 1 \\
1 & -1 & -1 & 1 & -1 & 1 & -1 & 1 \\
-1 & 1 & 1 & -1 & 1 & -1 & 1 & -1 \\
1 & -1 & -1 & 1 & 1 & -1 & 1 & -1 \\
\hline-1 & -1 & 1 & 1 & -1 & 1 & -1 & 1 \\
1 & 1 & -1 & -1 & 1 & -1 & 1 & -1 \\
-1 & -1 & 1 & 1 & -1 & 1 & -1 & 1 \\
1 & 1 & -1 & -1 & 1 & -1 & 1 & -1
\end{array}\right],
$$

while the second user generates his codewords based on the frequency arrangement $C_{2}$

$$
T_{2}^{+}=\left[\begin{array}{rrrr|rrrr}
1 & -1 & 1 & -1 & 1 & -1 & 1 & -1  \tag{15}\\
1 & -1 & 1 & -1 & -1 & 1 & -1 & 1 \\
-1 & 1 & -1 & 1 & -1 & 1 & -1 & 1 \\
-1 & 1 & -1 & 1 & 1 & -1 & 1 & -1 \\
\hline 1 & -1 & -1 & 1 & 1 & 1 & -1 & -1 \\
-1 & 1 & 1 & -1 & -1 & -1 & 1 & 1 \\
1 & -1 & -1 & 1 & 1 & 1 & -1 & -1 \\
-1 & 1 & 1 & -1 & -1 & -1 & 1 & 1
\end{array}\right], \quad T_{2}^{-}=\left[\begin{array}{rrrr|rrrr}
-1 & 1 & -1 & 1 & -1 & 1 & -1 & 1 \\
-1 & 1 & -1 & 1 & 1 & -1 & 1 & -1 \\
1 & -1 & 1 & -1 & 1 & -1 & 1 & -1 \\
1 & -1 & 1 & -1 & -1 & 1 & -1 & 1 \\
\hline-1 & 1 & 1 & -1 & -1 & -1 & 1 & 1 \\
1 & -1 & -1 & 1 & 1 & 1 & -1 & -1 \\
-1 & 1 & 1 & -1 & -1 & -1 & 1 & 1 \\
1 & -1 & -1 & 1 & 1 & 1 & -1 & -1
\end{array}\right] .
$$

Based on (12), the first user embeds a bit of information $d_{1, k}=1$, while the second user embeds a bit of information $d_{2, k}=-1$, as a result of which we get a steganographic message

$$
M_{k}=X_{k}+T_{1}^{+}+T_{2}^{-}=\left[\begin{array}{llllllll}
213 & 214 & 213 & 218 & 215 & 214 & 214 & 214  \tag{16}\\
212 & 217 & 215 & 216 & 217 & 212 & 218 & 212 \\
216 & 212 & 215 & 215 & 214 & 213 & 214 & 214 \\
215 & 215 & 218 & 215 & 212 & 216 & 212 & 216 \\
214 & 216 & 215 & 213 & 214 & 215 & 218 & 216 \\
214 & 212 & 215 & 217 & 216 & 218 & 212 & 216 \\
215 & 218 & 215 & 214 & 215 & 213 & 216 & 216 \\
214 & 214 & 215 & 216 & 215 & 217 & 214 & 215
\end{array}\right] .
$$

We note here that the degree of perturbation of the container image when embedding information by the developed method depends on the following factors: the number of users simultaneously transmitting the additional information, and specific values of the additional information bits.

Remark. In view of the fact that most of the images used today are represented using the RGB model, where 1 byte is allocated for encoding of each color (each color component is represented by numbers in the range $[0, \ldots, 255]$ ), in the case of the presence in the block of boundary values for this range ( 0 or 255 ), the mentioned block is not used in the process of steganographic transformation.

Let's move on to the information extraction algorithm.
Information Extraction Algorithm
Step 1. In accordance with the relationship between the two-dimensional and onedimensional Walsh-Hadamard transforms, each user $A_{z}$ of the steganographic system, in accordance with the frequency arrangement code issued to him, selects the rows of the WalshHadamard matrix $H_{N^{2}}$ of the order $N^{2}$, which are denoted as $\left\{h_{z, 1}\right\},\left\{h_{z, 2}\right\},\left\{h_{z, 3}\right\},\left\{h_{z, 4}\right\}$.

Step 2. The user finds the difference matrix of the steganographic message $M$ and the container image $X$, splits the resulting difference matrix into blocks $\Delta_{k}$ of size $\mu \times \mu$.

Step 3. The user divides each of the blocks of the difference matrix $\Delta_{k}$ into 4 sub-blocks of size $\frac{\mu}{2} \times \frac{\mu}{2}$, in accordance with the construction (5). By sequentially concatenating the rows, each of the resulting four subblocks is represented as a vector $\left\{\delta_{z, i}\right\}, i=\{1,2,3,4\}$ of length $\mu^{2}$.

Step 4. The user $A_{z}$ calculates the vector $P$ in accordance with the following formula

$$
\begin{gather*}
P_{z, k}=\left[\begin{array}{llll}
p_{1} & p_{2} & p_{3} & p_{4}
\end{array}\right], \\
p_{i}=\sum_{k=1}^{\mu^{2}} \delta_{j, k} h_{j, k}, i=\{1,2,3,4\} . \tag{17}
\end{gather*}
$$

Step 5. The user calculates the intended data bit embedded in the block $\Delta_{k}$ using the following formula

$$
\begin{equation*}
d_{z, k}=\operatorname{sign}\left(\sum_{i=1}^{4} p_{i}\right) \tag{18}
\end{equation*}
$$

As an example, let us extract the information embedded by the first and second users in the steganographic message (16). To do this, in accordance with the selected frequency arrangement codes, we form a set of Walsh functions for the first user

$$
\begin{align*}
& \left\{h_{1,1}\right\}=\left\{\begin{array}{llllllllllllllll} 
& 1 & -1 & -1 & +1 & -1 & +1 & +1 & -1 & +1 & -1 & -1 & +1 & -1 & +1 & +1
\end{array}-1\right\} ; \\
& \left\{h_{1,2}\right\}=\left\{\begin{array}{llllllllllllllll} 
& -1 & +1 & -1 & +1 & -1 & +1 & -1 & -1 & +1 & -1 & +1 & -1 & +1 & -1 & +1
\end{array}\right\} ; \\
& \left\{h_{1,3}\right\}=\left\{\begin{array}{llllllllllllllll} 
& +1 & -1 & -1 & -1 & -1 & +1 & +1 & +1 & +1 & -1 & -1 & -1 & -1 & +1 & +1
\end{array}\right\} ;  \tag{19}\\
& \left\{h_{1,4}\right\}=\left\{\begin{array}{llllllllllllllll} 
& -1 & -1 & -1 & -1 & +1 & -1 & +1 & +1 & -1 & +1 & -1 & -1 & +1 & -1 & +1
\end{array}\right\},
\end{align*}
$$

and also, for the second user

$$
\begin{align*}
& \left\{h_{2,}\right\}=\left\{\begin{array}{llllllllllllllll} 
& -1 & -1 & +1 & -1 & +1 & -1 & +1 & -1 & -1 & +1 & -1 & +1 & -1 & +1 & -1
\end{array}+1\right\} ; \\
& \left\{h_{2,2}\right\}=\left\{\begin{array}{lllllllllllllllll}
1 & -1 & +1 & -1 & -1 & +1 & -1 & +1 & -1 & +1 & -1 & +1 & +1 & -1 & +1 & -1
\end{array}\right\} ; \\
& \left\{h_{2,3}\right\}=\left\{\begin{array}{lllllllllllllllll} 
& +1 & -1 & -1 & +1 & -1 & +1 & +1 & -1 & +1 & -1 & -1 & +1 & -1 & +1 & +1 & -1
\end{array}\right\} ;  \tag{20}\\
& \left\{h_{2,4}\right\}=\left\{\begin{array}{llllllllllllllll} 
& +1 & +1 & -1 & -1 & -1 & -1 & +1 & +1 & +1 & +1 & -1 & -1 & -1 & -1 & +1
\end{array}+1\right\} .
\end{align*}
$$

Further, both users calculate the matrix of the difference between the steganographic message and the container image, and divide it into blocks of size $\mu \times \mu$. In the case of our example, the considered block will have the form

$$
\Delta_{k}=M_{k}-X_{k}=\left[\begin{array}{rrrrrrrr}
0 & 0 & -2 & 2 & 0 & 0 & 0 & 0  \tag{21}\\
-2 & 2 & 0 & 0 & 2 & -2 & 2 & -2 \\
2 & -2 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 2 & -2 & -2 & 2 & -2 & 2 \\
0 & 2 & 0 & -2 & 0 & -2 & 2 & 0 \\
0 & -2 & 0 & 2 & 0 & 2 & -2 & 0 \\
0 & 2 & 0 & -2 & 0 & -2 & 2 & 0 \\
0 & -2 & 0 & 2 & 0 & 2 & -2 & 0
\end{array}\right] .
$$

Based on the obtained matrix ${ }^{\Delta_{k}}$, the first and second users select the corresponding vectors $\left\{\delta_{z, i}\right\}, i=\{1,2,3,4\}$

$$
\begin{align*}
& \left\{\delta_{1,1}\right\}=\left[\begin{array}{llllllllllllllll}
0 & 0 & -2 & 2 & -2 & 2 & 0 & 0 & 2 & -2 & 0 & 0 & 0 & 0 & 2 & -2
\end{array}\right] ; \\
& \left\{\delta_{1,2}\right\}=\left[\begin{array}{llllllllllllllll}
0 & 0 & 0 & 0 & 2 & -2 & 2 & -2 & 0 & 0 & 0 & 0 & -2 & 2 & -2 & 2
\end{array}\right] ; \\
& \left\{\delta_{1,3}\right\}=\left[\begin{array}{llllllllllllllll}
0 & 2 & 0 & -2 & 0 & -2 & 0 & 2 & 0 & 2 & 0 & -2 & 0 & -2 & 0 & 2
\end{array}\right] ;  \tag{22}\\
& \left\{\delta_{1,4}\right\}=\left[\begin{array}{llllllllllllllll}
0 & -2 & 2 & 0 & 0 & 2 & -2 & 0 & 0 & -2 & 2 & 0 & 0 & 2 & -2 & 0
\end{array}\right] \text {. }
\end{align*}
$$

Further, using (17), as well as his own set of vectors $\left\{h_{1, i}\right\}$ (19), the first user calculates the vector ${ }^{P_{1, k}}$, as well as, in accordance with expression (18), the data bit intended for him

$$
P_{1, k}=\left[\begin{array}{llll}
16 & 16 & 16 & 16 \tag{23}
\end{array}\right] \rightarrow d_{1, k}=1
$$

Similarly, the vector ${ }^{P_{2, k}}$, as well as the intended data bit, is calculated by the second user

$$
P_{2, k}=\left[\begin{array}{llll}
-16 & -16 & -16 & -16 \tag{24}
\end{array}\right] \rightarrow d_{2, k}=-1 .
$$

## Characteristics of the developed multiple-access steganographic method

One of the most important properties of the developed steganographic method is the possibility of simultaneous operation of such a number of users, which is necessary at the given moment, with the total number $J$ of registered users, each of which has its own frequency arrangement.

Nevertheless, with an increase in the number of simultaneously operating users in the system, the information load on the image-container increases, and, accordingly, its quality deteriorates. As a measure of the quality of a steganographic message, we will take the PSNR [1] indicator, which is determined in accordance with the following formula

$$
\begin{equation*}
P S N R=20 \lg \left(\frac{255}{\sqrt{M S E}}\right) \tag{25}
\end{equation*}
$$

Where

$$
\begin{equation*}
M S E=\frac{1}{n m} \sum_{i} \sum_{j}|X(i, j)-M(i, j)|^{2} . \tag{26}
\end{equation*}
$$

In Fig. 1 a graph of the dependence of PSNR of steganographic messages on the number of simultaneously operating in the system users is shown.


Fig. 1. Graph of dependence of PSNR of steganographic message on the number of simultaneously operating users

To obtain this data, an experiment was performed using 500 lossless TIFF images from the NRCS database [12], into each of which information coming from a different number of users was embedded, after which the PSNR of the received steganographic message was measured.

The analysis of data displayed on Fig. 1 shows that an increase in the number of simultaneously operating users leads to a drop in the PSNR of a steganographic message, and this process is the same both for the case of using the frequency arrangement code based on the RS-code over the Galois field $G F(5)$ and over the Galois field $G F(13)$. Note that with the number of simultaneously operating users $N \leq 8$, the PSNR values remain at an acceptable level. In the case of using frequency arrangements based on the RS-code over the Galois field $G F(5)$, information is embedded into the high-frequency components, therefore, even with a value $P S N R \approx 30 \mathrm{~dB}$, the reliability of perception remains at a sufficient level, which can be clearly seen in Fig. 2.

Moreover, in Fig. 2 into the blue RGB component of an image of size $2592 \times 3872$ with a total number of shared channels $N=20$ we embedded in total a $20 \cdot 324 \cdot 484$ bits $=3136320$ bits $=382.85 \mathrm{~KB}$ of information.


Fig. 2. An example of a steganographic message with embedded information from $N=20$ users (a), as well as the original container (b)

Subjective ranking of the images shown in Fig. 2 does not reveal any artifacts or visual differences from the original container image in the steganographic message.

A property of asynchronous address communication systems, which is reflected in the developed steganographic method with multiple access, is the presence of intra-system interference: forming into a common stream, pulses of other channels can accidentally form a code combination of a given channel, leading to the appearance of a corresponding interference. Another type of intra-system noise is interference suppression and nonlinear pulse suppression.

The experiments performed show that intra-system interference appears when the number of users simultaneously operating in the system exceeds the value ${ }^{q}$. In Fig. 3 we show the dependence of the number of errors (in \%) occurring in the communication channel (channel of each of the users) depending on the number of users operating in the system for frequency arrangement codes based on RS-codes over the Galois fields $G F(5)$ and $G F(13)$.


Fig. 3. Graphs of the dependence of the percentage of errors resulting from intra-system interference on the number of users

Analysis of the data presented in Fig. 3 shows that frequency arrangements based on the RS-code over the Galois field $G F(5)$ allow simultaneous operation of $N=5$ users without the occurrence of intra-system interference, while frequency arrangements based on the RS-code over the Galois field $G F(13)$ allow simultaneous operation of $N=13$ users without the occurrence of intra-system interference, however, even for values of the number of simultaneously operating users $N=20$ for these frequency arrangements (Table 2), the level of intra-system interference remains acceptable, and the number of errors that occur does not exceed $3.7 \%$.

## Conclusions

Let us note the main results obtained in this paper:

1. In contrast to the well-known analogs that perform code division of channels regardless of the embedding of information into the container, in this paper we developed a fully-fledged steganographic method with multiple access based on code control and frequency arrangements. The developed steganographic method that provides the separate embedding (absence of the embedding) of information by each user at any time which is convenient for him using a personal frequency arrangement. It is proposed to use RS-codes over the Galois fields $G F(5)$ and $G F(13)$ as the frequency arrangement codes, which ensure the maximum reliability of perception and the largest number of simultaneously operating users.
2. The characteristics of the developed method are researched, within the framework of which it is shown that the PSNR of the resulting steganographic message depends on the number of users simultaneously transmitting information through the steganographic channel. With the number of simultaneously operating users $N \leq 8$, the PSNR values remain at an acceptable level. The existence of intra-system interference in the steganographic channel was detected with the number of simultaneously transmitting information users $N>q$. However, in the case of using frequency arrangements based on RS-codes over the Galois field $G F(13)$ with the number of users $N=20$, the number of errors generated by intra-system interference does not exceed $3.7 \%$.
3. The developed steganographic method is a rational solution if it is necessary to organize a steganographic channel with multiple access and can provide flexible resource allocation: the operation of the required number of users with a given bandwidth (by allocating several communication channels to individual users) and the necessary reliability of perception (by increasing or reducing the number of simultaneously operating users).

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# СТЕГАНОГРАФІЧНИЙ МЕТОД МНОЖИННОГО ДОСТУПУ НА ОСНОВІ КОДОВОГО УПРАВЛІННЯ ТА ЧАСТОТНИХ РОЗСТАНОВОК 

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Розвиток, а також ширше практичне застосування сучасної стеганографії призводить до необхідності створення стеганографічних методів з множинним доступом, які могли б забезпечити одночасну передачу і розділення у стеганографічному каналі інформації від декількох користувачів. Відомі на сьогоднішній день стеганографічні методи з множинним доступом засновані на технології MC-CDMA і не показують, як саме має відбуватися вбудовування та вилучення додаткової інформації. Метою цієї статті є розробка стеганографічного методу з множинним доступом на основі кодового управління та частотних розстановок. Поставлена мета була досягнута за рахунок розробки стеганографічного методу з кодовим управлінням та застосуванням частотних розстановок на основі двічі циклічних кодів Ріда-Соломона над полями Галуа GF(q), що забезпечує роздільне вбудовування інформації кожним користувачем у будь-який зручний для нього час з використанням особистої частотної розстановки. При цьому частотні розстановки запропоновано будувати за допомогою PC -кодів над полями $\mathrm{GF}(5)$ i GF(13). Досліджено характеристики розробленого методу, в рамках чого показано, що PSNR результуючого стеганоповідомлення залежить від кількості користувачів, що одночасно передають інформацію через стеганографічний канал. При кількості одночасно працюючих абонентів $\mathrm{N} \leq 8$, значення PSNR залишаються на допустимому рівні. Під час роботи запропонованого стеганографічного методу виявлено виникнення внутрішньосистемних перешкод у стеганографічному каналі при кількості абонентів $\mathrm{N}>\mathrm{q}$, що одночасно передають інформацію, однак при використанні частотних розстановок на основі РС-коду над полем $\mathrm{GF}(13)$, їх вплив є несуттєвим при практично обгрунтованій кількості каналів, що розділяються. Розроблений стеганографічний метод $\epsilon$ раціональним рішенням у разі необхідності організації стеганографічного каналу з множинним доступом і може забезпечити гнучкий розподіл ресурсів: роботу потрібної кількості абонентів із заданою пропускною здатністю та необхідною надійністю сприйняття.
Ключові слова: стеганографія, кодове управління, множинний доступ, кодове розподілення каналів, частотні розстановки.

